

## Chapter 5 Exercises: Trams

This exercise shows formally that the conclusions of the Trams example are very sensitive to an arbitrary prior upper bound  $M$ , which was not apparent from a single WinBUGS run. This problem can be alleviated by using the Jeffreys prior.

- a) Suppose we bound the uniform distribution above by  $M$ , say 5000. What is the posterior distribution?
- b) What is the posterior mean  $E[N|y]$ ?
- c) Calculate an approximation to  $\sum_{N=y}^M \frac{1}{N}$ , by assuming  $N$  is continuous and approximating the sum by an integral. Thus obtain a simplified expression for the posterior mean.
- d) Show that the posterior mean increases as  $M/\log M$ , thus we can make it as big as we want by increasing  $M$ .
- e) Under the Jeffreys prior, show that as  $M$  goes to infinity the posterior median tends to a fixed quantity. First derive the posterior distribution, and then solve  $p(N \leq n|y) = 0.5$  for  $n$ .